

# Qualitative Comparative Analysis

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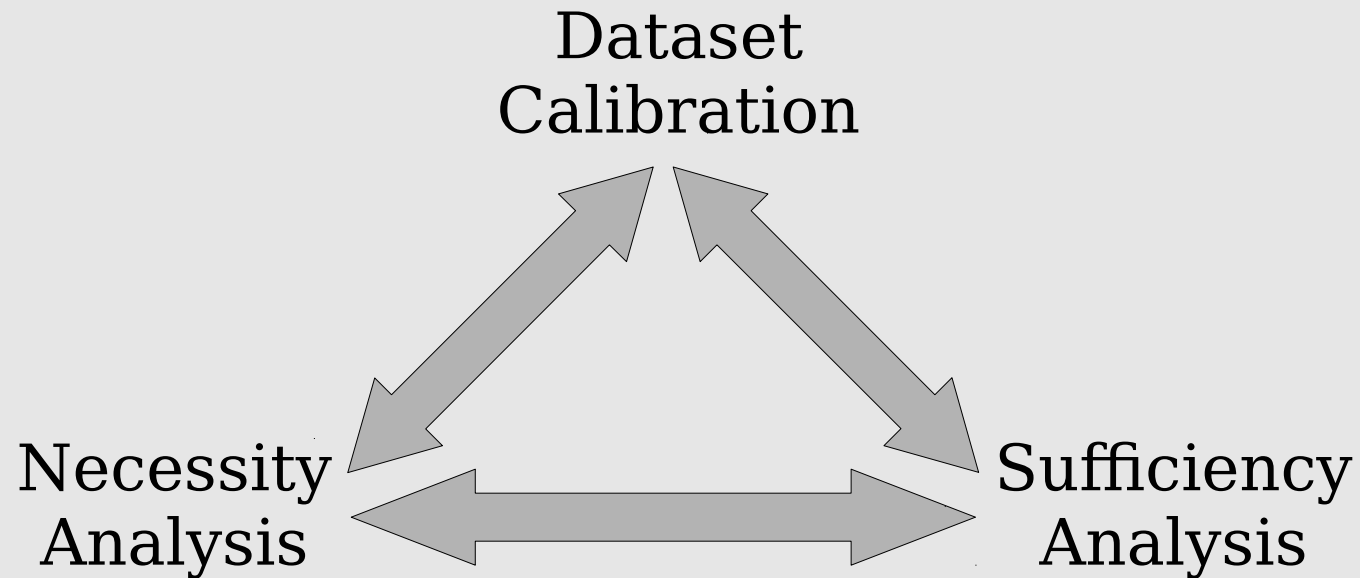
# Overview

- Day 1: Introductions and overview
  - Review of QCA resources, publications, and software
  - QCA as an investigation of invariance
  - Three analytic components of QCA: dataset calibration, necessity analysis, and sufficiency analysis
  - Three types of QCA projects: identifying causal recipes, uncovering taxonomies, understanding context
  - Discussion of research projects
- Day 2: Nuts and bolts—QCA in depth
  - Dataset calibration
  - Necessity analysis
    - Consistency and coverage measures for necessity
    - Testing for necessary conditions
  - Sufficiency analysis
    - Consistency and coverage measures for sufficiency
    - Constructing and reducing truth tables
    - Interrogating the analysis and deriving solutions
- Day 3: Putting it all together
  - Conducting a step-wise QCA analysis
  - Writing up and presenting QCA research
  - Discussion of research projects

# Boolean Algebra

- UPPERCASE for the presence of a condition
- lowercase for the absence/negation of a condition
- Negation
$$\sim A = 1 - A$$
$$a = 1 - A$$
- Logical and (Boolean multiplication)
$$A * b = Ab = \min(A, b)$$
- Logical or (Boolean addition)
$$A + b = \max(A, b)$$

# Three Analytic Components of QCA





# Calibrating Datasets

# Dataset Calibration

- Instrument calibration is routine in the natural sciences; largely absent in the social sciences.
- Social sciences emphasize relative effects: Paul is poorer than Peter; the United States is more democratic than North Korea.
- Calibration allows us to state that an individual is poor or that a country is democratic.
- Calibration requires application of theoretical and substantive knowledge.

# Calibrating Fuzzy Sets

Crisp set	Three-value fuzzy set	Four-value fuzzy set	Six-value fuzzy set	Continuous fuzzy set
1 = fully in	1 = fully in	1 = fully in	1 = fully in	1 = fully in
	0.67 = more in than out	0.67 = more in than out	0.8 = mostly but not fully in  0.6 = more or less in	Degree of membership is more "in" than "out" $0.5 < X < 1$
----- 0.5 = Crossover Point -----				
		0.33 = more out than in	0.4 = more or less out  0.2 = mostly but not fully out	Degree of membership is more "out" than "in" $0.0 < X < 0.5$
0 = fully out	0 = fully out	0 = fully out	0 = fully out	0 = fully out

# Calibrating Fuzzy Sets

- Manual calibration vs “direct” and “indirect” methods
- Fuzzy sets are asymmetrical
- Fuzzy sets vs crisp-sets
- Fuzzy sets vs multi-valued sets vs dummy variables



# Analyzing Necessary Conditions

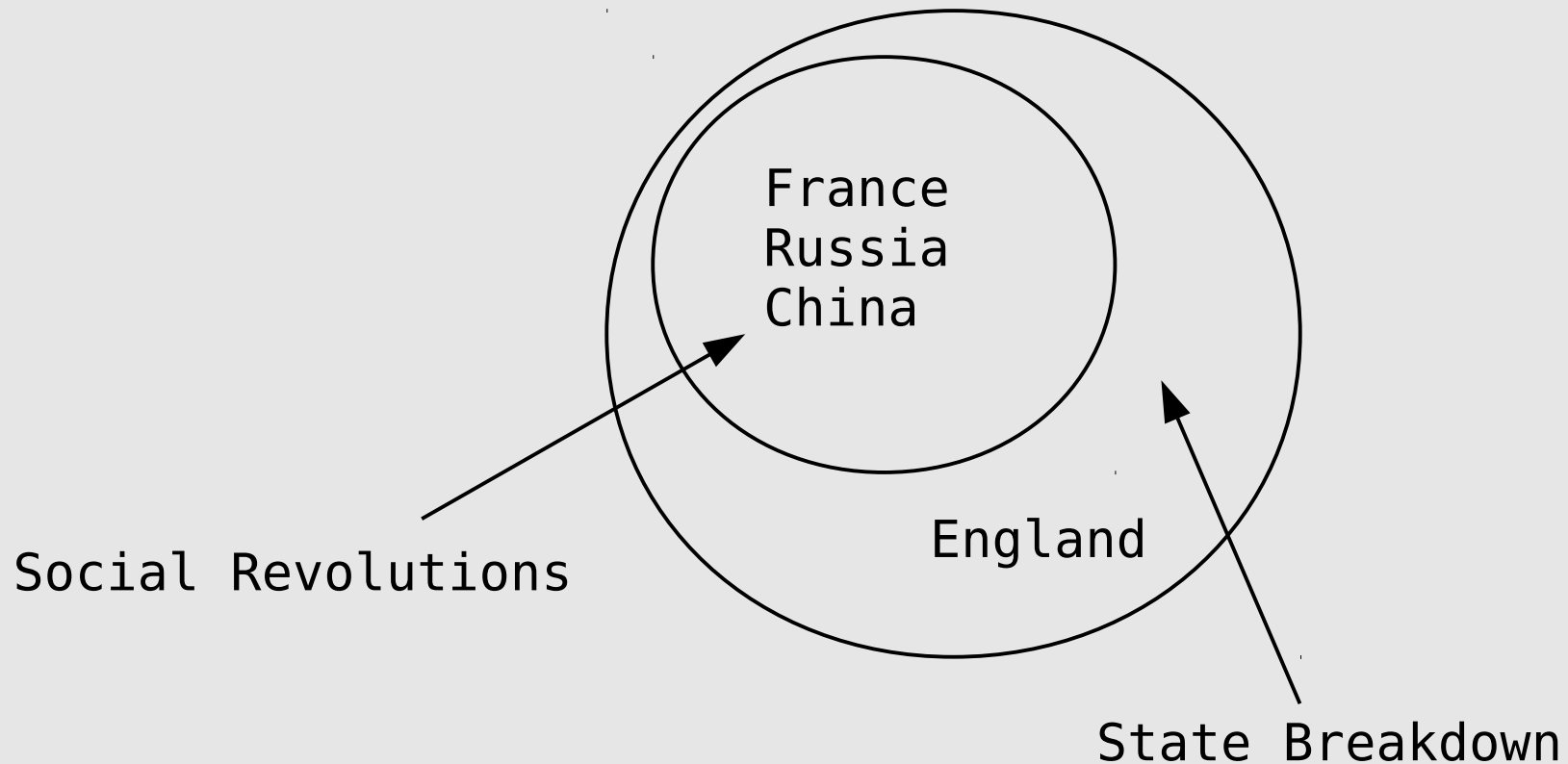
# Necessity Analysis

- Underdeveloped in the literature; QCA development has focused on sufficiency analysis
- *Kirq* and *acq* have sophisticated necessity testing

# Necessary Conditions

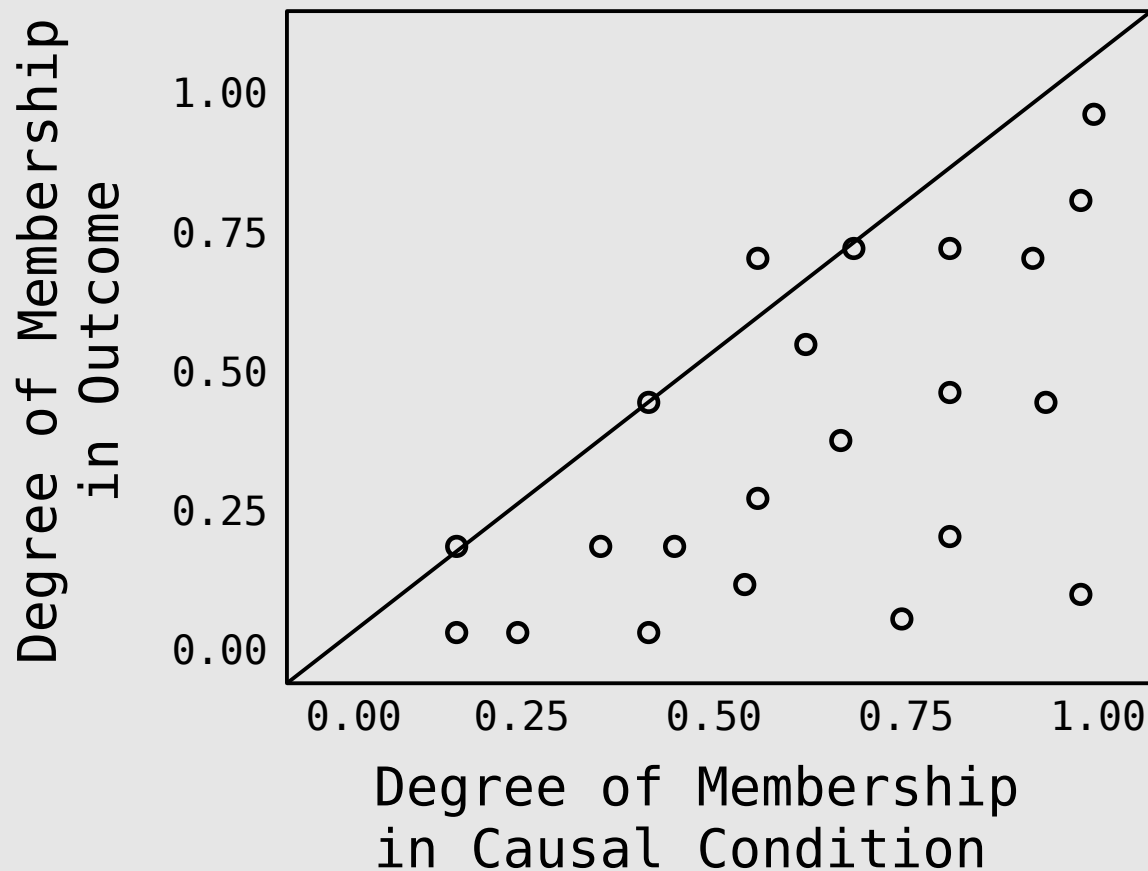
Causal condition must (almost always) be present for outcome to occur.

Outcome is a subset of Cause



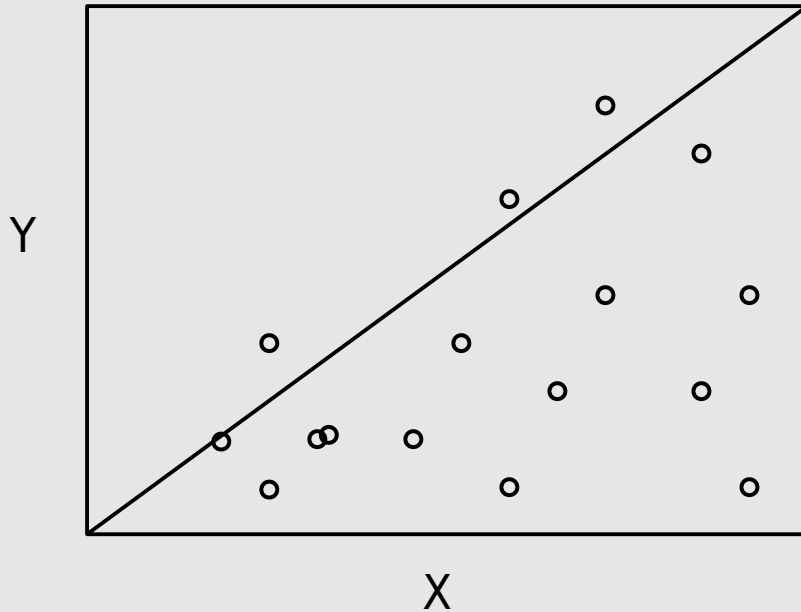
# Fuzzy Subset Relationship Consistent with Necessity

Outcome is a subset of Cause ( $X \geq Y$ )

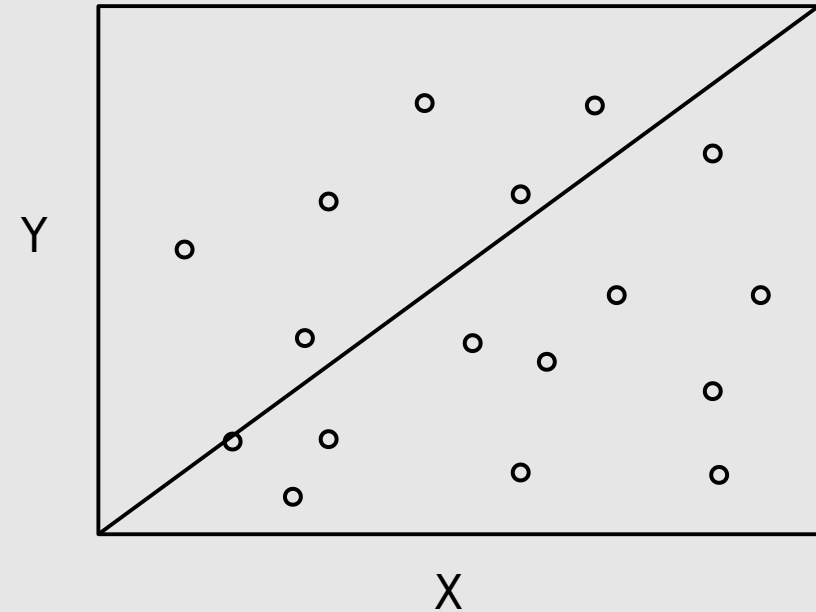


# Assessing Necessary Conditions

- *Consistency* measures degree to which subset relationship is “consistent” with necessity



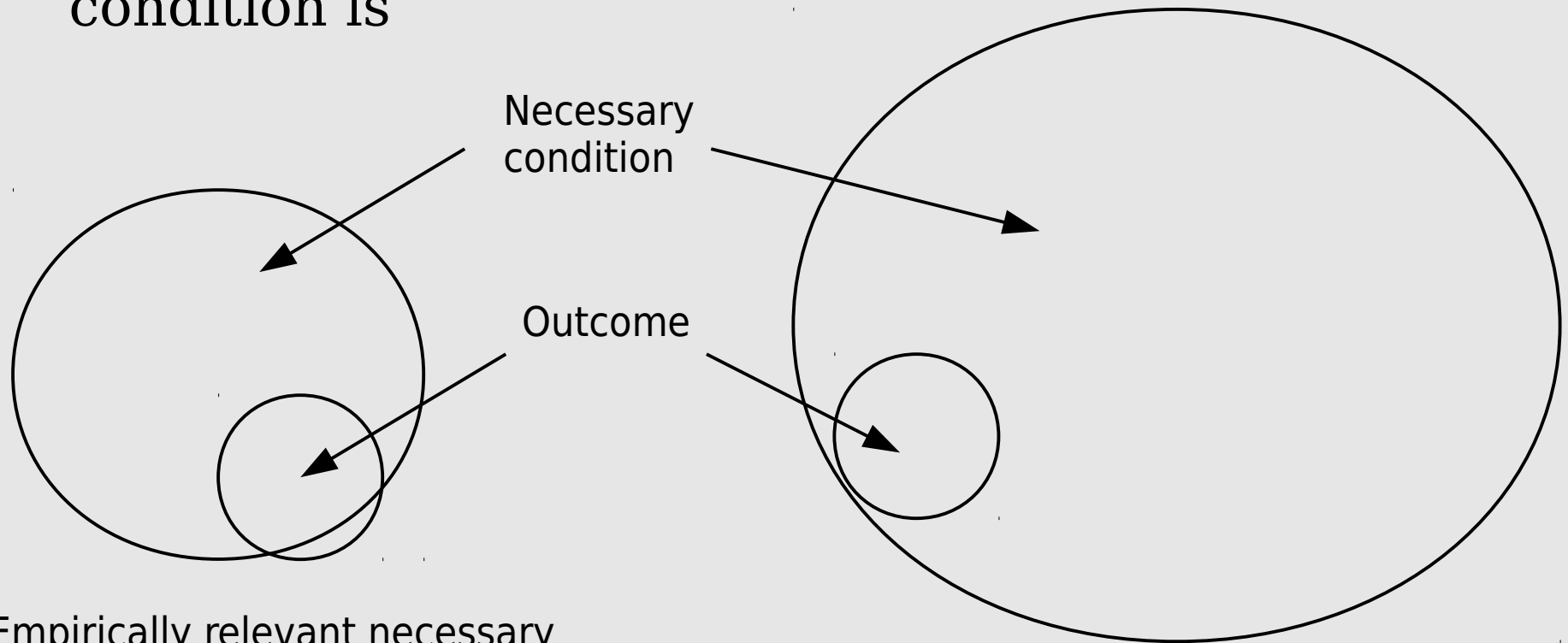
Subset relationship consistent with necessity



Subset relationship with substantial inconsistency

# Assessing Necessary Conditions

- *Coverage* measures how “relevant” a necessary condition is

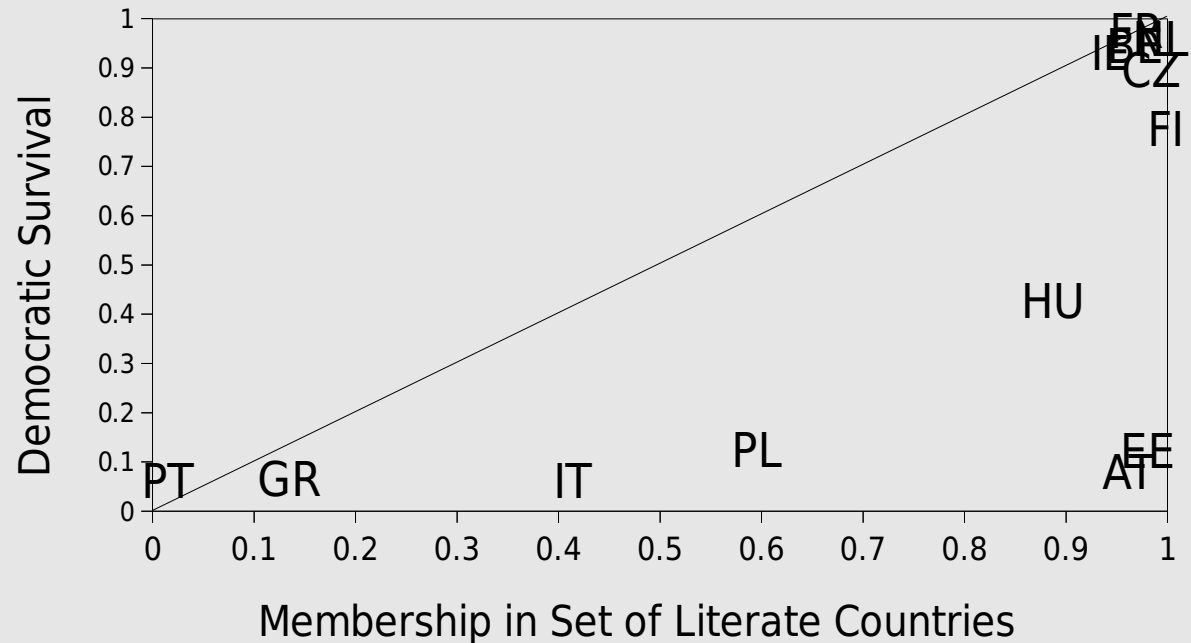


Empirically relevant necessary condition (high consistency)

Empirically irrelevant necessary condition (perfect consistency)

# Testing for Necessary Conditions

Obs	Dev	Urb	Lit	Sur
AT	.81	.12	.99	.05
BE	.99	.89	.98	.95
CZ	.58	.98	.98	.89
EE	.16	.07	.98	.12
FI	.58	.03	.99	.77
FR	.98	.03	.99	.95
DE	.89	.79	.99	.05
GR	.04	.09	.13	.06
HU	.07	.16	.88	.42
IE	.72	.05	.98	.92
IT	.34	.10	.41	.05
NL	.98	1.00	.99	.95
PL	.02	.17	.59	.12
PT	.01	.02	.01	.05



Term	Consis	Cov
LIT	0.99	0.58
Solution	0.99	0.58

# Testing for Necessary Conditions

- Assess consistency before coverage
- Join terms with logical or (e.g.,  $A+B+C$ )
- Many solutions are possible
- Use of theory is crucial



# Analyzing Sufficient Conditions

# Sufficiency Analysis

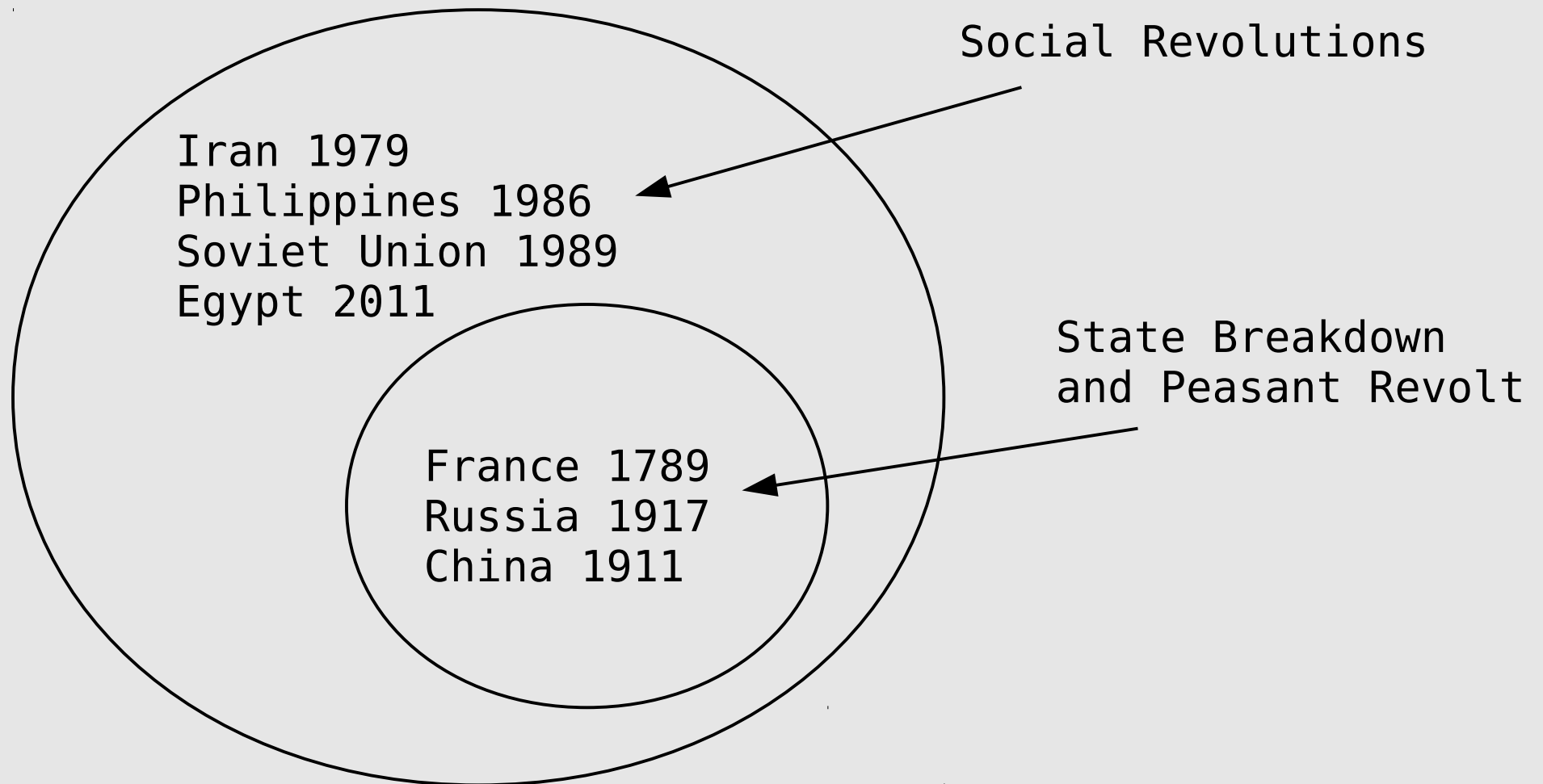
- More mature than necessity analysis; QCA development—and applications—have focused on sufficiency analysis
- Emphasis on causal complexity (a.k.a., multiple conjunctural causation, “recipes,” equifinality, or INUS conditions)

Feature	fs/QCA	Kirq & acq
Based on RSI Algorithms	✓	✓
Complex Solutions	✓	✓
Intermediate Solutions	✓	
Parsimonious Solutions	✓	✓
Impossible Conditions		✓
Contradictions		✓

# Sufficient Conditions

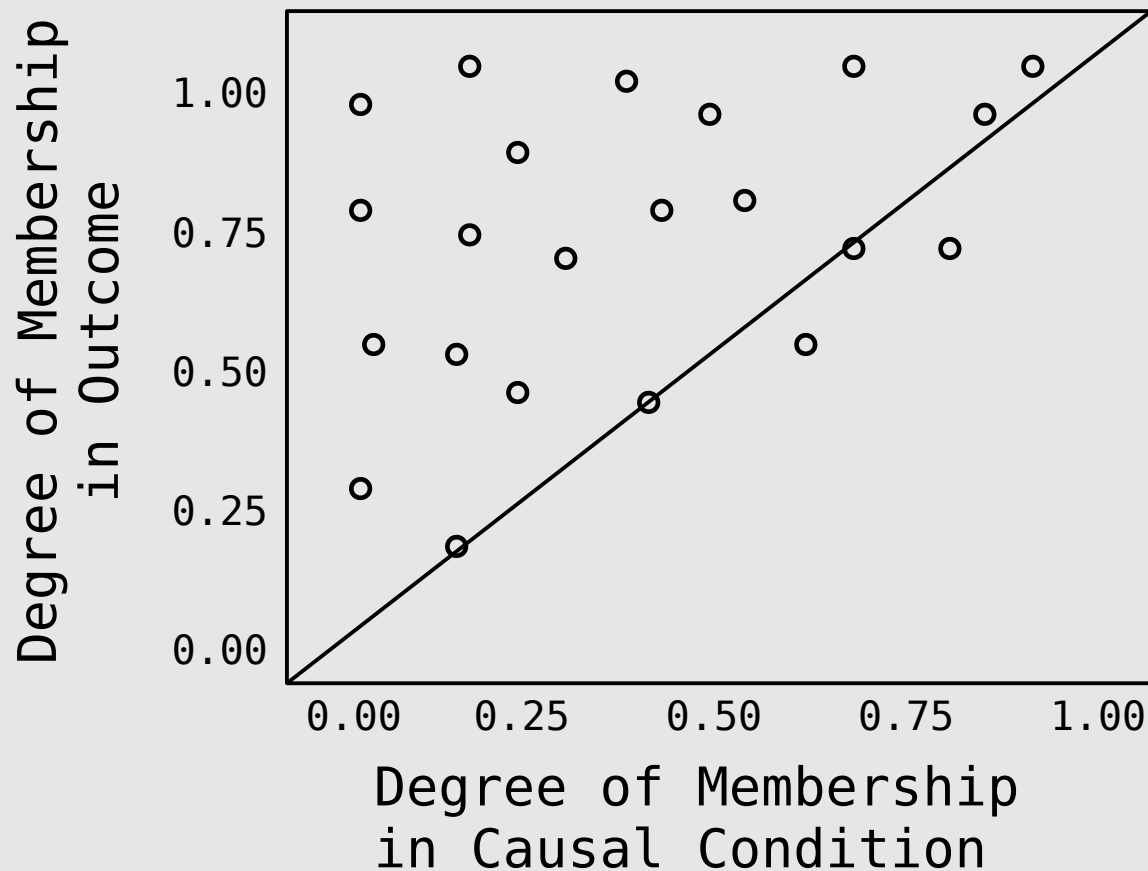
Outcome (almost) always occurs when causal condition is present.

Cause is a subset of Outcome



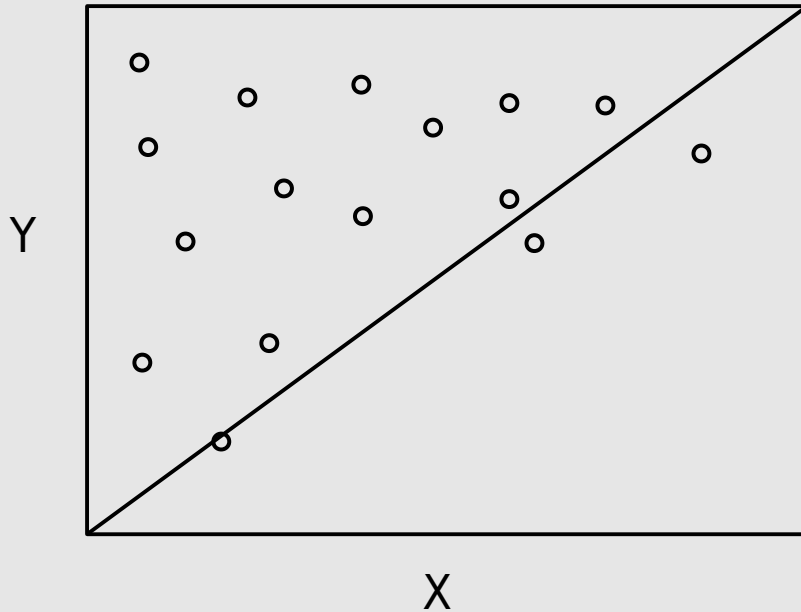
# Fuzzy Subset Relationship Consistent with Sufficiency

Cause is a subset of Outcome ( $Y \geq X$ )

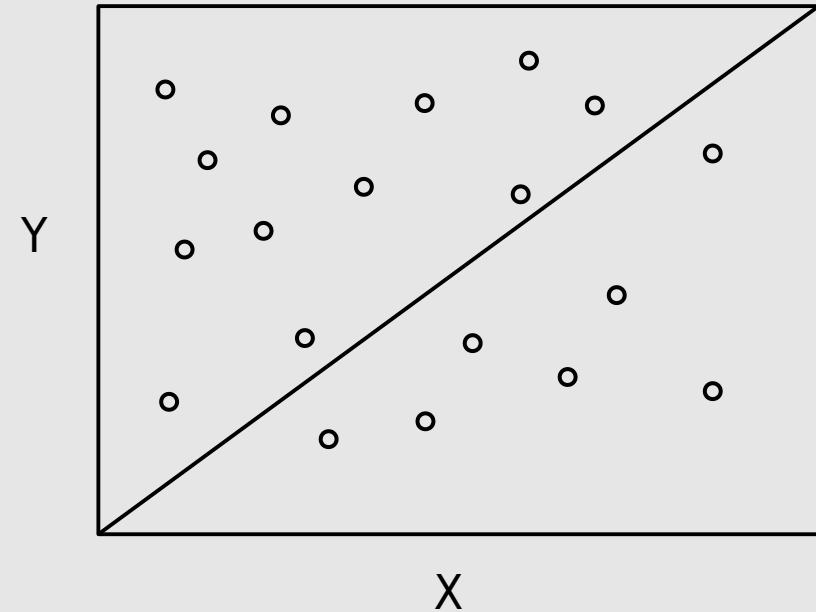


# Assessing Sufficient Conditions

- *Consistency* measures degree to which subset relationship is “consistent” with sufficiency



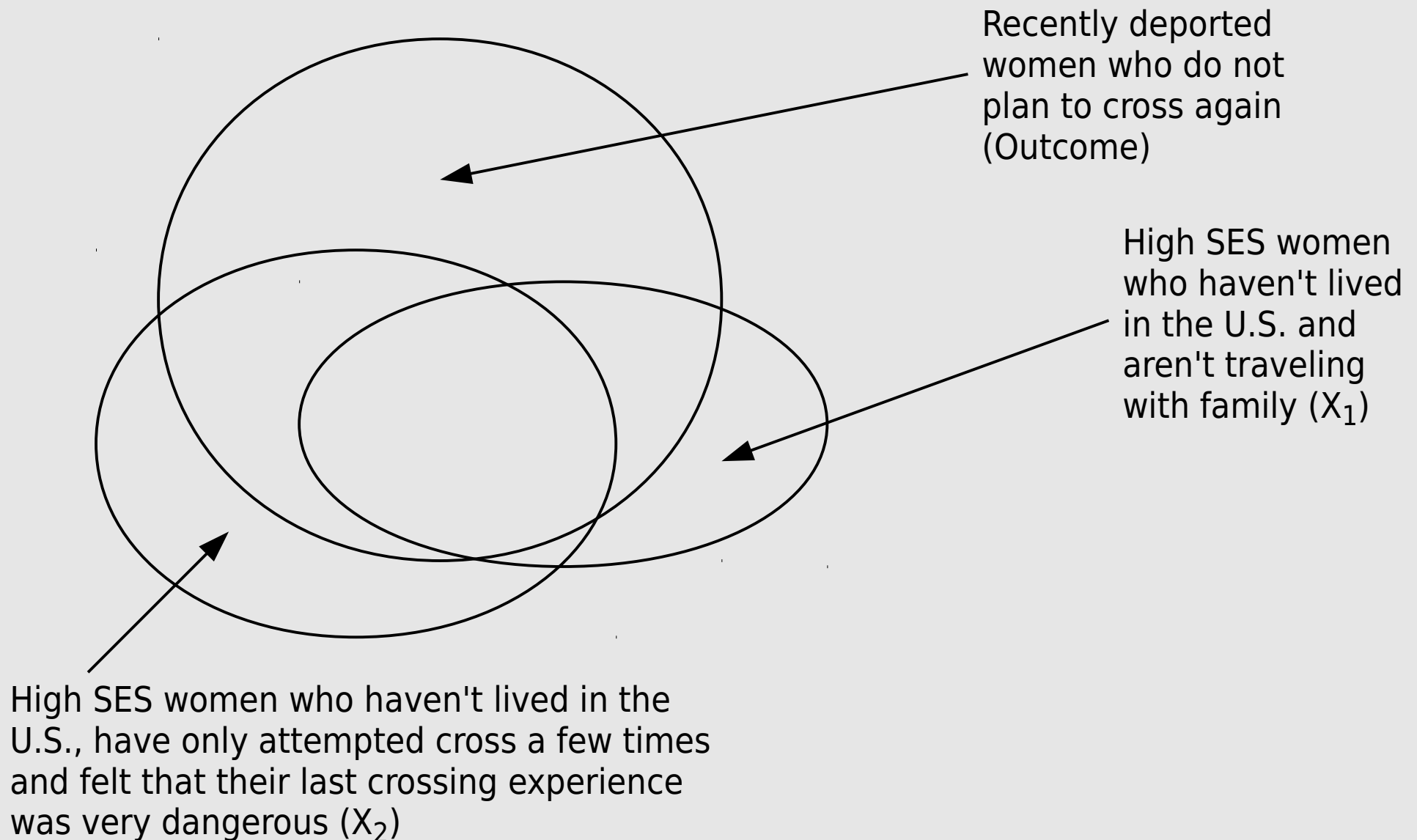
Subset relationship consistent with sufficiency



Subset relationship with substantial inconsistency

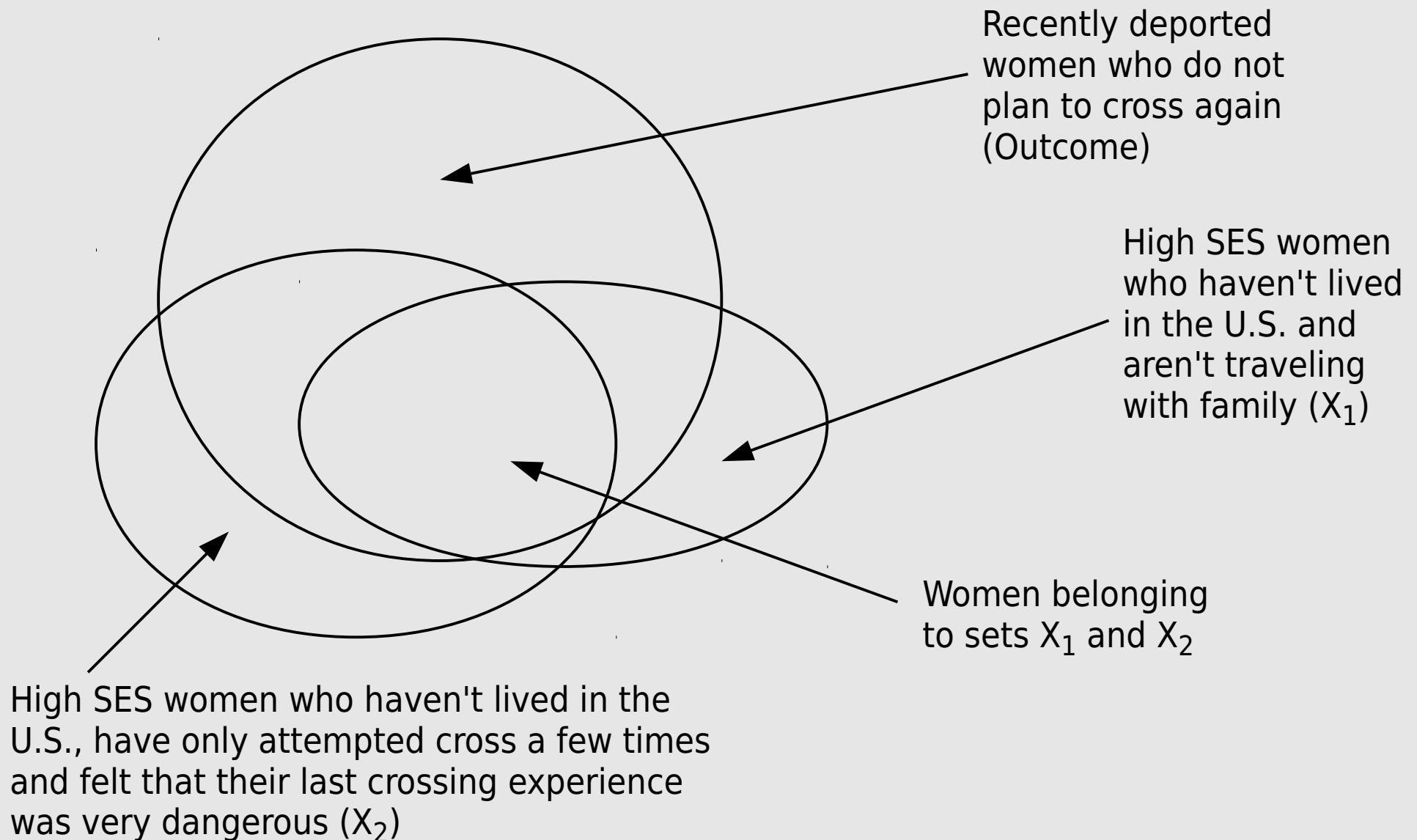
# Assessing Sufficient Conditions

- *Coverage* measures the relative “importance” of each solution



# Assessing Sufficient Conditions

- *Coverage* measures the relative “importance” of each solution



# Testing for Sufficient Conditions

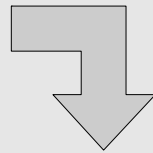
Term	Consis	Raw Cov	Uniq Cov
HISES*liveus*travfam +	0.90	0.32	0.13
HISES*liveus*numcross*DANGER	0.82	0.48	0.26
Solution	0.86	0.58	



# Truth Table Construction

Truth table algorithm sorts observations into types

Obs	Dev	Urb	Lit	Brk
AT	.81	.12	.99	.95
BE	.99	.89	.98	.05
CZ	.58	.98	.98	.11
EE	.16	.07	.98	.88
FI	.58	.03	.99	.23
FR	.98	.03	.99	.05
DE	.89	.79	.99	.95
GR	.04	.09	.13	.94
HU	.07	.16	.88	.58
IE	.72	.05	.98	.08
IT	.34	.10	.41	.95
NL	.98	1.00	.99	.05
PL	.02	.17	.59	.88
PT	.01	.02	.01	.95



	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE		BE, CZ, NL	
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT		FI, FR, IE	
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL		HU	
8	F	F	F	0.99	T	GR, IT, PT			

# Reading Truth Tables

Truth table assesses consistency between types and outcome

Democracy usually did not break down in countries that were (a) developed, urbanized, and literate (row 1) or (b) developed, not urbanized, and literate (row 3).

Democracy usually did break down in countries that were (c) not developed, not urbanized, and literate (row 7) or (d) not developed, not urbanized, and not literate (row 8)

	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE		BE, CZ, NL	
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT		FI, FR, IE	
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL		HU	
8	F	F	F	0.99	T	GR, IT, PT			

# Reading Truth Tables

Remainders are logically possible conditions lacking empirical instances

Remainders



	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE		BE, CZ, NL	
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT		FI, FR, IE	
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL		HU	
8	F	F	F	0.99	T	GR, IT, PT			

# Invariance in Truth Tables

	Dev	Urb	Consis	Y	Consis Obs	Inconsis Obs
1	T	T	0.41	F	DE	BE, CZ, NL
2	T	F	0.51	F	AT	FI, FR, IE
3	F	T	—	—		
4	F	F	0.89	T	EE, GR, IT, PL, PT	HU

	Dev	Urb	Lit	Consis	Y	Consis Obs	Inconsis Obs
1	T	T	T	0.41	F	DE	BE, CZ, NL
2	T	T	F	—	—		
3	T	F	T	0.51	F	AT	FI, FR, IE
4	T	F	F	—	—		
5	F	T	T	—	—		
6	F	T	F	—	—		
7	F	F	T	0.83	T	EE, PL	HU
8	F	F	F	0.99	T	GR, IT, PT	

# Reducing Truth Tables to Boolean Equations

To Primitive Expressions:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb*LIT +	0.83	0.42	0.27	EE, PL, [HU]
dev*urb*lit	0.99	0.40	0.24	GR, IT, PT
Solution	0.88	0.66		

# Reducing Truth Tables to Boolean Equations

To Primitive Expressions:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb*LIT +	0.83	0.42	0.27	EE, PL, [HU]
dev*urb*lit	0.99	0.40	0.24	GR, IT, PT
Solution	0.88	0.66		

To Prime Implicants:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

# Reducing Truth Tables to Boolean Equations

Reduce Prime Implicants (Complex Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

# Reducing Truth Tables to Boolean Equations

Reduce Prime Implicants (Complex Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

Reduce Prime Implicants Using Remainders (Parsimonious Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev	0.82	0.73	0.73	EE, PL, GR, IT, PT, [HU]
Solution	0.82	0.73		



# Constructing Intermediate Solutions

Complex Solution

Acsir +  
ACSir +  
ASIR

Parsimonious Solution

i +  
SR

Intermediate Solution #1

Ai +  
ACSi +  
ASR



Ai +  
ASR

Intermediate Solution #2

Air +  
ASIR

# Factoring Results

Initial Solution:

$$\begin{aligned} & \text{ELECTIONS} * \text{POLICE} + \\ & \text{urban} * \text{POLICE} + \\ & \text{CONFLICT} * \text{ELECTIONS} * \text{URBAN} + \\ & \text{CONFLICT} * \text{elections} * \text{urban} + \\ & \text{conflict} * \text{ELECTIONS} * \text{urban} \end{aligned}$$

Factored Solution:

$$\begin{aligned} & \text{POLICE} (\text{ELECTIONS} + \text{urban}) + \\ & \text{URBAN} (\text{CONFLICT} * \text{ELECTIONS}) + \\ & \text{urban} ((\text{CONFLICT} * \text{elections}) + (\text{conflict} * \text{ELECTIONS})) \end{aligned}$$